

Note: In this problem set, expressions in green cells match corresponding expressions in the text answers.

```
Clear["Global`*"]
```

5 - 11 Principal value Ln z. Find Ln z when z equals

5. - 11

```
Log[-11]
```

$i\pi + \text{Log}[11]$

7.  $4 - 4I$

```
ComplexExpand[Log[4 - 4 i]]
```

$-\frac{i\pi}{4} + \frac{\text{Log}[32]}{2}$

```
N[%]
```

$1.73287 - 0.785398 i$

9.  $0.6 + 0.8I$

```
Log[0.6 + 0.8 i]
```

$0. + 0.927295 i$

11.  $E I$

```
Log[e i]
```

$1 + \frac{i\pi}{2}$

12 - 16 All Values of Log x. Find all values and graph some of them in the complex plane.

13.  $\text{Log}[1]$

```
ComplexExpand[Log[1]]
```

0

According to numbered line (3) on p. 637,  $\text{Log}[z] = \text{Log}[z] \pm 2n\pi i$ . The extra factor is ignored by Mathematica however, since the software only concerns itself with the principal

value.

$$15. \text{Log}[e^i]$$

$$\text{Log}[e^i]$$

$i$

$$\text{Log}[\text{Abs}[e^i]] + i \text{Arg}[e^i]$$

$i$

$$\text{ComplexExpand}[\text{Log}[\text{Abs}[e^i]] + i \text{Arg}[e^i]]$$

$i$

Mathematica's system of presenting only the principal value of the complex number works against me here. I would have liked to have found a way to get Mathematica to tack on a  $2n\pi i$  factor, which would make it match the text answer.

$$17. \text{ Show that the set of values of } \text{Log}[i^2] \text{ differs from the set of values of } 2 \text{Log}[i].$$

$$\text{Log}[\text{ComplexExpand}[i^2]]$$

$i \pi$

$$2 \text{ComplexExpand}[\text{Log}[i]]$$

$i \pi$

Mathematica is not responsive.

$$18 - 21 \text{ Equations. Solve for } z.$$

$$19. \text{Log}[z] = 4 - 3i$$

$$\text{Solve}[\text{Log}[z] == 4 - 3i, z]$$

$$\{\{z \rightarrow e^{4-3i}\}\}$$

$$\text{dis} = e^4 e^{-3i}$$

$$e^4 e^{-3i}$$

$$\text{ComplexExpand}[\text{dis}]$$

$$e^4 \text{Cos}[3] - i e^4 \text{Sin}[3]$$

$$21. \text{Log}[z] = 0.6 + 0.4i$$

$$\text{Clear}["\text{Global`*}"]$$

```
Solve[Log[z] == 0.6 + 0.4 I, z]
{{z -> 1.67828 + 0.709566 i}}
```

```
rib = e0.6 e0.4 i
```

```
1.67828 + 0.709566 i
```

I don't know how to make Mathematica cough up Euler's identity, so the symbolic version of the answer is not here.

22 - 28 General Powers. Find the principal value.

23.  $(1 + i)^{1-i}$

```
Clear["Global`*"]
```

```
ComplexExpand[(1 + i)1-i]
```

$$\sqrt{2} e^{\pi/4} \cos\left[\frac{\pi}{4} - \frac{\text{Log}[2]}{2}\right] + i \sqrt{2} e^{\pi/4} \sin\left[\frac{\pi}{4} - \frac{\text{Log}[2]}{2}\right]$$

```
Simplify[%]
```

$$(1 + i) e^{\pi/4} \left( \cos\left[\frac{\text{Log}[2]}{2}\right] - i \sin\left[\frac{\text{Log}[2]}{2}\right] \right)$$

The above cell contains Euler's identity but the text answer does not.

$$(1 + i) e^{\frac{\pi}{4}} e^{-\frac{\text{Log}[2]}{2} i}$$

$$(1 + i) 2^{-\frac{i}{2}} e^{\pi/4}$$

```
N[%]
```

```
2.80788 + 1.31787 i
```

25.  $(-3)^{3-i}$

```
Clear["Global`*"]
```

```
ComplexExpand[(-3)3-i]
```

$$-27 e^{\pi} \cos[\text{Log}[3]] + 27 i e^{\pi} \sin[\text{Log}[3]]$$

```
Simplify[%]
```

$$-27 e^{\pi} (\cos[\text{Log}[3]] - i \sin[\text{Log}[3]])$$

```
N[%]
```

```
-284.179 + 556.431 i
```

The numeric equivalent scores, but the text symbolic answer is not what Mathematica comes up with.

$$27. (-1)^{2-i}$$

```
Clear["Global`*"]
```

```
ComplexExpand[(-1)^(2-i)]
```

```
eπ
```

```
N[%]
```

```
23.1407
```